

Nuclear Chemistry

Handwritten Notes

for **NTA NET-JRF / GATE**

written by *Gaurav Mishra*

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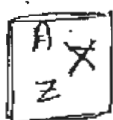
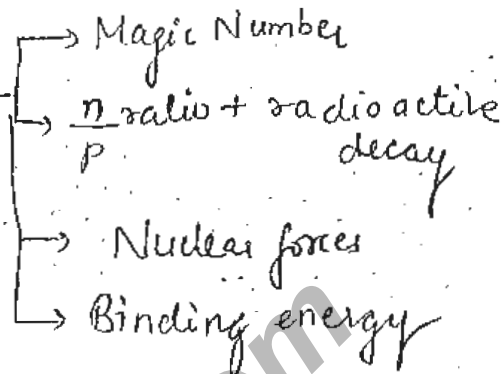
TopicsNuclear Chemistry

(2-6 marks)

GATE → 1 or 2 Ques

BARC → 10-12 Ques

- Nuclear size
- Iso series
- Stability of Nuclei (Very imp)
- Kinetics of Radioactive decay
- Radioactive dating
- Threshold energy, B.E, Q-value
- Neutron Activation Analysis



Proton = Z

Proton + Neutron = A (Mass No.)

Neutron = A - Z

units:

Radius of atom = $A \cdot (10^{-10} \text{ m})$

" + Nuclei = fermi (10^{-15} m)

- Distance b/w proton and neutrons in nucleus is 2-3 fermi

- Activation energy non zero for chemical rxn and activation energy zero for nuclear chemistry.

- No chemical change, only nuclear change, no e^- involvement

$$R = R_0 A^{1/3}$$

$$R_0 = \text{constant } (1.4 \times 10^{-15} \text{ m})$$

$$A = \text{mass no.}$$

$$R = \text{radius of Nuclei}$$

$$1 \text{ Barn} = 10^{-28} \text{ m}^2$$

Isotope	Isobar	Isotone	Isodiapher	Nuclear Isomer	Iso-electronic
same atomic number ${}^{12}\text{C}, {}^{13}\text{C}, {}^{14}\text{C}$	same mass number ${}^{40}_{18}\text{Ar}, {}^{40}_{19}\text{K}$	same neutron number ${}^3_1\text{H}, {}^4_2\text{He}$	different element have same isotopic number (n-p) ${}^{19}_9\text{F}, {}^{39}_{19}\text{K}$ $(A-2Z) \propto (n-p)$ $p+n-p-p = (n-p)$ $19-2 \times 9 \quad 39-19 \times 2$ $(1) \quad (1)$	Same element but diff nuclear stability ${}^{60}_{27}\text{Co}^+, {}^{60}_{27}\text{Co}$ ↓ High energy less stable Metastable	H, He^+ Isosteric Same no. of e ⁻ same atomicity $\text{CO}_2 \quad \text{N}_2\text{O}$ $(22e^-) \quad (22e^-)$

first 5, are involved in nuclear chemistry.

28th Oct, 2016

Stability of Nuclei :-

Proton no. =>	Even	Even	Odd	Odd
Neutron no. =>	Even	odd	even	odd
Stability =>	59%	20%	19%	2%
Magic no. =>	2, 8, 20, 28, 50, 82			

It represents closed shell of nucleon

Nuclear forces

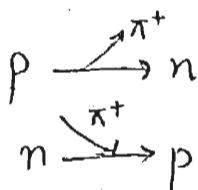
Attractive forces are stronger than repulsive forces.

It means forces involved in the nucleus is not electrostatic. Nuclear forces exist in neutron-neutron, proton-proton, neutron-proton by π Meson exchange

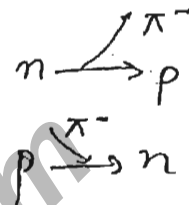
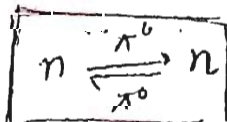
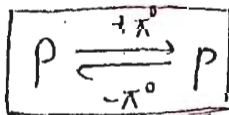
Rate of exchange of π -Meson is 10^{24} sec^{-1} which both

Three π Mesons $\rightarrow \pi^+, \pi^0, \pi^-$

Mass of Mesons = $273 \times$ Mass of e^-



$p \rightleftharpoons n + \pi^+$



$n \rightleftharpoons p + \pi^-$

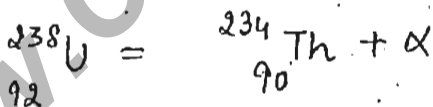
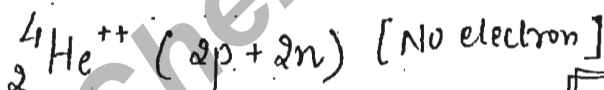
Radioactivity decay and n/p ratio :

Radioactive discovered by Henry Becquerel

Unstable nuclei emit sub atomic particle spontaneously until it becomes a stable nuclei.

Unstable nuclei \rightarrow Radioactive
 Stable nuclei \rightarrow Not radioactive

α -decay

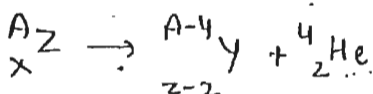


$${}^A_Z X \rightarrow {}^{A-4}_{Z-2} Y + {}^4_2\text{He}$$

$n: n \rightarrow n-2$
 $p: p \rightarrow p-2$

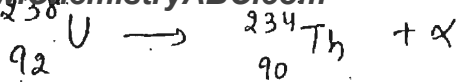
$\frac{n}{p} = \frac{n-2}{p-2}$

$\Rightarrow \frac{n-2}{p-2} - \frac{n}{p} = \frac{2(n-p)}{p(p-2)} \Rightarrow \frac{n}{p} \uparrow$ i.e.



$(A-2Z) \quad A-4-2(Z-2)$
 $A-4-2Z+4 = (A-2Z)$

Iso diapher

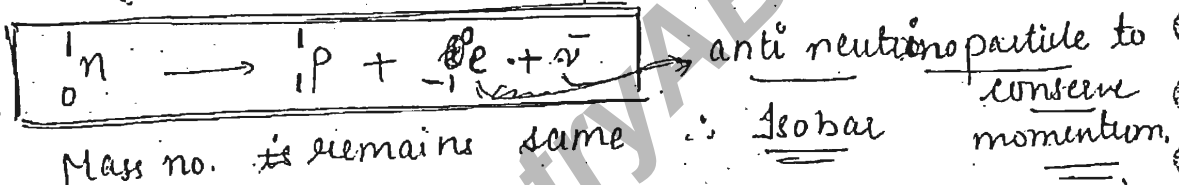


- ⇒
- $\frac{n}{p}$ ↑ ses
 - Isodiapher (daughter ~~is~~ parent)
 - Nuclear fission
 - ← (2 left shift)

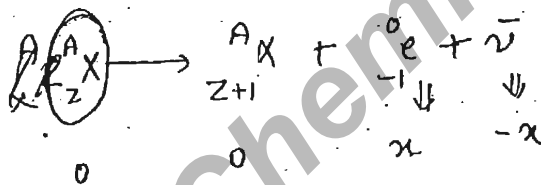
If α -decay occurs in closed vessel, then ideal behaviour of gas is considered, (i.e. STP conditions or $PV = nRT$)

B-decay

neutron converts to proton and electron



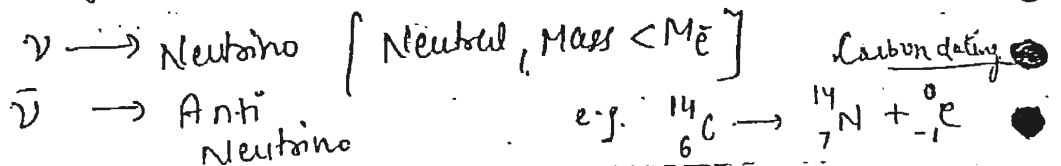
- Mass no. remains same ∴ isobar
- 1 Right shift



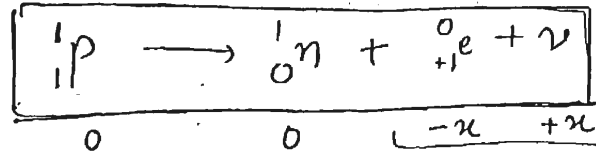
$$\frac{n}{p} = \frac{n-1}{p+1} \Rightarrow \frac{n-1}{p+1} - \frac{n}{p} = -\frac{(n+p)}{p(p+1)}$$

$\frac{n}{p}$ ↓ ses

One neutron converts into proton by β -decay. Mass no. remains same. So parent and daughter are isobar. Always associated with emission of anti neutrino particle to conserve momentum. One right shift by daughter element takes place.



Positron decay
(β^+)

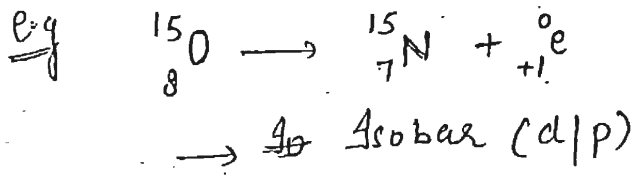


equal and opp momentum



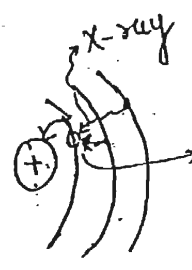
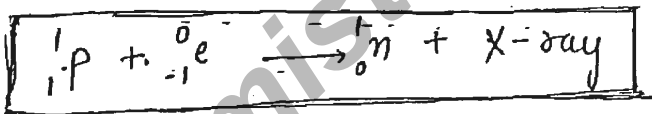
$$\frac{n}{p} \quad \frac{n+1}{p-1} \quad \frac{n+1}{p-1} - \frac{n}{p} = \frac{(n+p) +ve}{(p(p-1)) - +ve}$$

$$\frac{n}{p} \uparrow \text{ses}$$

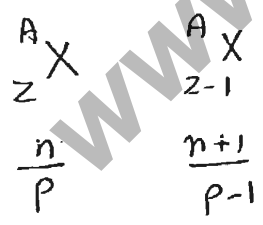


K-Capture

electron from filled shell falls over nucleus, if proton is converted into neutron. If \bar{e} belongs to K shell, then it is called K-capture. If \bar{e} belongs to L shell, then it is called L-capture.

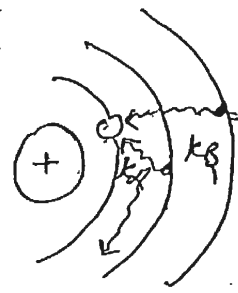


hole created by falling of \bar{e} into nucleus. then other \bar{e} from other shell fulfills this vacancy and X-ray is emitted.



$$\frac{n+1}{p-1} - \frac{n}{p} = \frac{(n+p) +ve}{(p(p-1))}$$

$$\frac{n}{p} \uparrow \text{ses}$$



- \rightarrow Isobars (d/p)
- \rightarrow One left shift \leftarrow
- \rightarrow X-ray emitted.

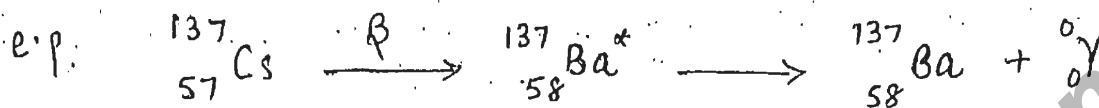
K-capture is happening because nucleus is unstable.

Radioactivity is a spontaneous process.

γ-decay

γ-decay never occure independently. It always occure in association with α or β decay.

By α or β decay, atom gets excited, then come back by emission of quanta of light in the form of EMR.

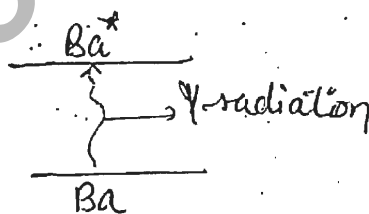


→ $\frac{n}{p}$ ratio do not change

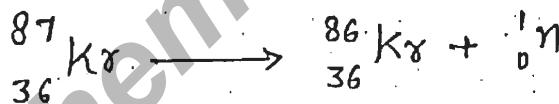
→ Nuclear isomer (d/p)

→ No shift in periodic table

→ γ-radiation

Neutron emission

(Very rare)



$$\frac{n}{p}$$

$$\frac{n-1}{p}$$

$$\frac{n-1}{p} - \frac{n}{p} =$$

$$\frac{-1}{p} \left\{ \frac{n \text{ uses}}{p} \right\}$$

→ $\frac{n}{p}$ ↓ uses

→ d/p are p isotopes

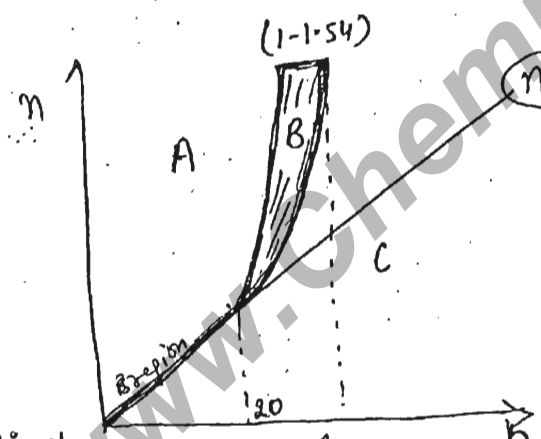
→ Neutron emit

→ No shift

Decay	Relation	Z	A	shift	n/p ratio	Associated product
α	Isodiapher	-2	-4	$\leftarrow\leftarrow$	+ (1.5e)	Nil
β^-	Isobar	+1	0	\rightarrow	- (1.5e)	$\bar{\nu}$
β^+	Isobar	-1	0	\leftarrow	+	ν
K-capture	Isobar	-1	0	\leftarrow	+	γ -ray
γ	Isomer	0	0	No shift	No change	γ -ray
Neutron	Isotope	0	-1	No shift	-	Nil

$\frac{n}{p}$ ratio \rightarrow Minimum value = 0 $\quad {}^1_1\text{H} \quad \frac{0}{1} = 0$
 Maximum value = 2 $\quad {}^3_1\text{H} \quad \frac{2}{1} = 2$

if $\frac{n}{p}$ ratio lies b/w $1 - 1.54$ then stable



A region (unstable region)

$$\left(\frac{n}{p}\right)_A > \left(\frac{n}{p}\right)_B$$

\Rightarrow All isotope undergo β^- -decay.

B region (stable region)
 $\frac{n}{p} = 1 - 1.54$
 Stable Belt

C region (unstable region)

$$\left(\frac{n}{p}\right)_C < \left(\frac{n}{p}\right)_B$$

$\frac{n}{p}$ ratio of C region can be used by, α -decay \rightarrow Radioisotope of natural heavy nuclei

β^+ \rightarrow radioisotope of lighter element

K-capture \rightarrow radioisotope of Artificial Heavy element.

Kinetics of Radioactive decay

Acc to Law of Radioactive decay, rate of radioactive decay is directly proportional to the no. of radioactive atoms.

$$r \propto N$$

$$r = \lambda N \quad \lambda = \text{Decay constant}$$

λ does not depend on temp, pressure, external field, depends only on nature of nuclei.

$$\text{Activity} = r = -\frac{dN}{dt} = \lambda N$$

↓
No. of radioactive atom decaying per unit time

$$\Rightarrow N = N_0 e^{-\lambda t}$$

$$\ln \frac{N_0}{N} = \lambda t$$

$$\text{Specific Activity} = \frac{\text{Activity}}{\text{Mass}}$$

for stable isotope, $\lambda = 0$
e.g. (^{12}C)

No. of Half lives

$$\lambda t = \ln \frac{N_0}{N} \quad \text{--- (1)}$$

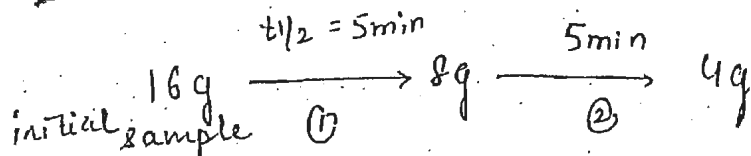
$$\lambda t_{1/2} = \ln \frac{N_0}{N_0/2}$$

$$\lambda t_{1/2} = \ln 2 \quad \text{--- (2)}$$

$$\frac{(1)}{(2)} \quad \frac{\lambda t}{\lambda t_{1/2}} = \frac{\ln N_0/N}{\ln 2}$$

A → product
 $t=0, N_0$
 $t=t, N$
 $t=t_{1/2}, \frac{N_0}{2}$

$$\text{No. of half lives (n)} = \frac{\text{total time}}{\text{Half life time}}$$



$$\text{No. of half lives (n)} = \frac{\text{total time}}{t_{1/2}} = \frac{10}{5} = \text{②}$$

Dividing eqn ① by ② we get $\boxed{n} = \frac{t}{t_{1/2}} = \frac{\ln N_0/N}{\ln 2}$

$$n \ln 2 = \ln \frac{N_0}{N}$$

$$\ln 2^n = \ln \frac{N_0}{N} \Rightarrow \boxed{2^n = \frac{N_0}{N}}$$

$$\Rightarrow \boxed{\frac{N}{N_0} = \left(\frac{1}{2}\right)^n}$$

Average life (τ)

Species reduce to 37.1% of its original life value

$$\lambda t = \ln \frac{N_0}{N} \Rightarrow \lambda \cdot \tau = \ln \frac{100}{37} = 1$$

$$\tau = \frac{1}{\lambda}$$

$\lambda, \tau, t_{1/2} \Rightarrow$ Intensive property.

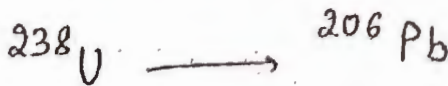
In duration

$$\lambda(t_2 - t_1) = \ln \frac{N_1}{N_2}$$

Radioactive decay

^{238}U (used for detecting age of rock etc. rock and mountain)

^{14}C (Wood and Mummy)
 $t_{1/2} = 5730 \text{ years}$



$t=0$ 1 mole
 $t=t$ 0.1 mole

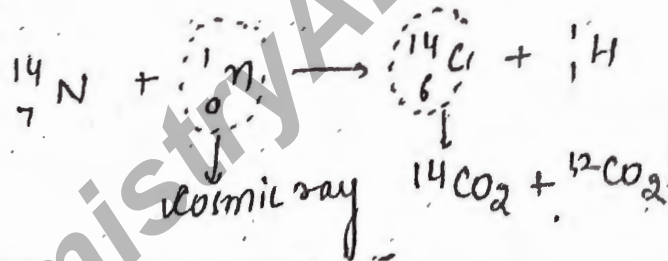
$N_0 = (U^{238} + Pb^{206})_t$

$N = (U^{238})_t$

$\lambda t = \ln \frac{N_0}{N} \Rightarrow \frac{0.693 t}{t_{1/2}} = \ln \frac{(U^{238} + Pb^{206})_t}{(U^{238})_t}$

^{14}C Carbon dating

In atmosphere,

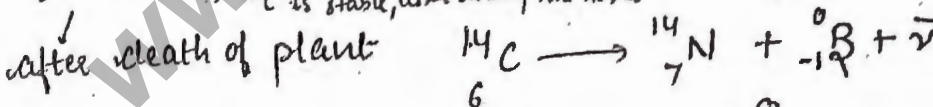


$\frac{^{14}\text{C}}{^{12}\text{C}} = \text{constant} \rightarrow$ In atmosphere / plant

At $t=0$ $^{12}\text{C} = x$ $^{14}\text{C} = y$ $\frac{y}{x} = \text{constant}$

$t=t$ $^{12}\text{C} = x$ $^{14}\text{C} = y'$ $\frac{y'}{x} = \text{constant}$

Here $y' < y$



Decay of ^{14}C is β decay

$\frac{n}{p} = \frac{8}{6} = 1.3$ $\frac{n}{p} = \frac{7}{7} = 1$

$\frac{n}{p}$ ratio of $^{14}_7\text{N} < n/p$ ratio of $^{14}_6\text{C} \Rightarrow \beta$ decay

Now $\ln \frac{N_0}{N} = \lambda t \Rightarrow \ln \left(\frac{y}{x} \right)_{t=0} = \lambda t$
 $\left(\frac{y'}{x} \right)_{t=t}$

$\ln \frac{y}{y'} = \lambda t$

Here $\lambda = 0.693 / t_{1/2}$
 and $t_{1/2} (^{14}\text{C}) = 5730 \text{ yrs}$

In atmosphere, cosmic ray smash into normal ^{12}C atoms (in atmosphere $^{12}\text{CO}_2$) and create ^{14}C isotopes (in atmosphere $^{14}\text{CO}_2$) this process occur for a long time and constantly, so there is fairly constant ratio of $^{14}\text{C}/^{12}\text{C}$ by ^{12}C in atmosphere. Now living plants breathe CO_2 indiscriminately and so while they are living and have constant ratio of $\frac{^{14}\text{C}}{^{12}\text{C}}$ in ~~it ^{14}C and ^{12}C~~ them as atmosphere. humans also consume plants so they have same ratio of $\frac{^{14}\text{C}}{^{12}\text{C}}$ as present in atmosphere as in living plants. When they die, ratio does not remain constant \therefore of β -decay and amount of ^{14}C goes and hence ratio of $^{14}\text{C}/^{12}\text{C}$ also goes. No change in amount of ^{12}C (\because no disintegration) and finally we can evaluate the age of wood or ~~any~~ mummy.

Q 16g of radioactive sample have $t_{1/2} = 4\text{ hours}$
How much sample remain after 10 hours .

Soln $16\text{g} \xrightarrow{4\text{hr}}$

$$kt = \ln \frac{N_0}{N}$$

$$\frac{0.693}{4} \times 10 = \ln \frac{16}{N} \Rightarrow 1.7325 = \ln \frac{16}{N}$$

$$2.82\text{g}$$

Specific Activity \rightarrow Intensive
Activity \rightarrow Extensive

$N = 2.82g$

Ques A radioactive nuclei A undergo α decay to produce B. Half life of decay of A is 69.32 yrs. After what time $\frac{\text{weight of A}}{\text{weight of B}}$ becomes $\frac{0.204}{1}$



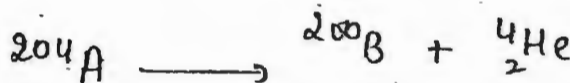
$kt = \ln \frac{N_0}{N}$

$\frac{0.693}{69.32} t = \ln \left(\frac{N_A/M_A}{N_B/M_B} \right)$
 $= \ln \left(\frac{0.204 \times 200}{1 \times 204} \right)$

$\therefore W_A = 0.204$
 $W_B = 1$
 $M_A = 204$
 $M_B = 200$

$\frac{N_A}{N_B} = \frac{W_A/M_A}{W_B/M_B} = \frac{W_A}{W_B} \cdot \frac{M_B}{M_A}$

$= \frac{0.204}{1} \times \frac{200}{204 \times 1000} = \frac{0.2}{10} = \left(\frac{1}{5}\right)$



$t = 0 \quad 6$
 $t = t \quad 1$

$\Rightarrow \frac{N_0}{N} = \frac{6}{1}$

$\Rightarrow kt = \ln \frac{N_0}{N} \Rightarrow \frac{0.693}{69.32} t = \ln \frac{6}{1}$

$t = \frac{1.791}{0.0099}$

$t = 180 \text{ years}$

Units of radioactivity

$$1 \text{ Bq} = 1 \text{ dps (S.I)}$$

$$1 \text{ Rd} = 10^6 \text{ dps}$$

$$1 \text{ Curie} = 3.7 \times 10^{10} \text{ dps}$$

Difference b/w physical and chemical adsorption is classified by the behaviours of N_2 on iron surface. At the temp. of liquid $\text{N}_2 = 190^\circ\text{C}$, N_2 is adsorbed physically on the iron surface. Amount of Nitrogen adsorbed decreases rapidly as the temp. raises. At R.T, Fe does not adsorb nitrogen at all. At high temp. i.e. 500°C Nitrogen is chemically adsorbed on the Fe surface.

Binding Energy

Energy released when a nucleus is formed by the combination of proton and neutron is called binding energy.

$$B.E = \Delta m c^2$$

$$\downarrow$$

$$\text{kg (ms}^{-1}\text{)}^2$$

$$\text{kg m}^2 \text{s}^{-2}$$

$$\text{kg m}^2 \text{s}^{-2} \cdot \text{m}$$

$$\text{Nm}$$

$$\text{Joule}$$

$$B.E = \Delta m \times 931.5 \text{ MeV}$$

$$\downarrow$$

$$\text{amu}$$

$$1 \text{ a.m.u} = \frac{1}{12} \times \text{Mass of } ^{12}\text{C atom}$$

$$= \frac{1}{12} \times \frac{12}{N_A}$$

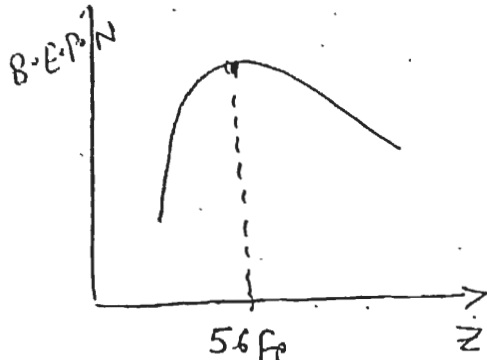
$$= \frac{1}{N_A} = 1.66 \times 10^{-27} \text{ kg}$$

$$1 \text{ MeV} = 1.6 \times 10^{-13} \text{ J}$$

NA atom = 1 mole - 1 g
 1 atom = $\frac{12}{NA}$

$\Delta m = \text{mass defect}$

Binding energy per nucleon :-



(Most stable) high B.E./N due to

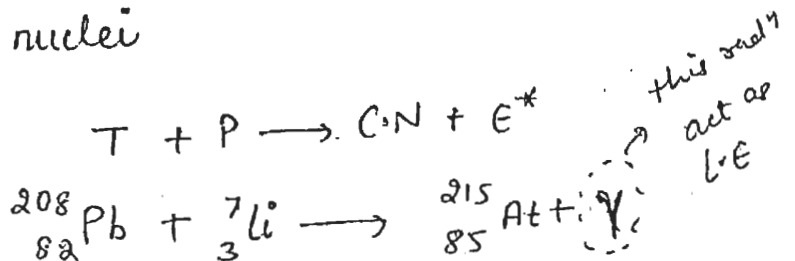
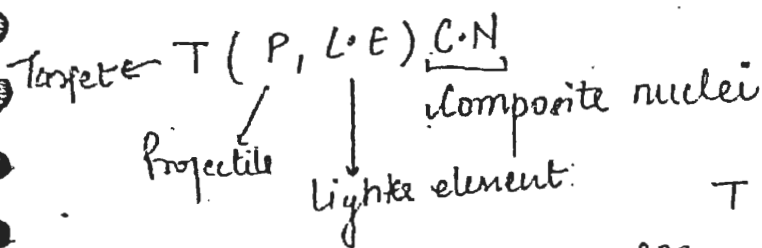
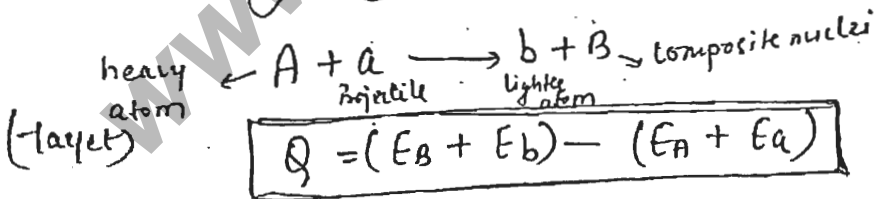
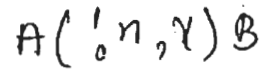
Q-value of Nuclear Reaction expressed in terms of incoming and outgoing kinetic energy.

$Q = +ve$	exoergic
$Q = -ve$	endoergic

* \rightarrow Bethe's Notation



Neutron capture \rightarrow



Since Q value comes -ve, it means by Gaurav Mishra
 energy must be converted into mass for a
 reaction to occur.

$Q = +ve$ exoergic \Rightarrow mass convert into $k.e$

$Q = -ve$ endoergic \Rightarrow $k.e$ convert into mass

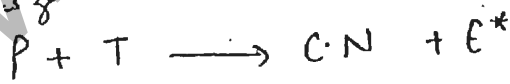
Threshold energy (E_{th})

minimum kinetic energy of the projectile needed
 to initiate the reaction is called threshold
 energy. In other words, minimum projectile
 energy necessary to satisfy mass energy and
 momentum conservation in nuclear rxn, to form
 products in their ground state.
 $-ve$ Q value necessary to compensate for a
 $-ve$ Q value.

Excitation energy (E^*) \rightarrow

It is the excess energy above the ground state
 for which the product of nuclear rxn.

E^* is at rest
 $\therefore E^* = E_{total} - E_{rest}$



Mass Energy Conservation

$$E_p + m_p c^2 + m_T c^2 = E_{C.N} + m_{C.N} c^2 + E^*$$

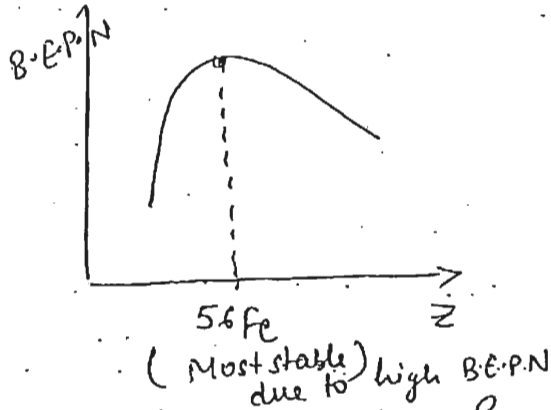
$$E_p + \underbrace{(m_p + m_T - m_{C.N})}_{Q} c^2 = E_{C.N} + E^*$$

$$\therefore \boxed{E_p + Q = E_{C.N} + E^*} \quad - (1)$$

$1 \text{ atom} = \frac{12}{\text{NA}}$

$\Delta m = \text{mass defect}$

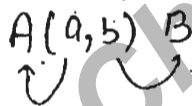
Binding energy per nucleon :-



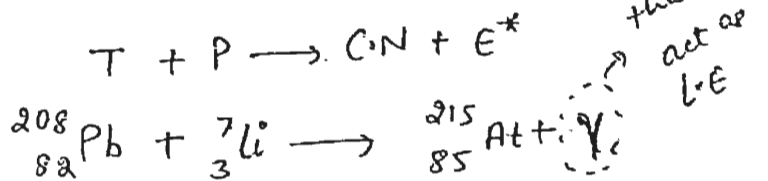
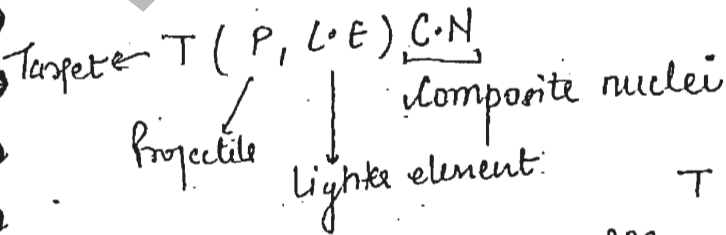
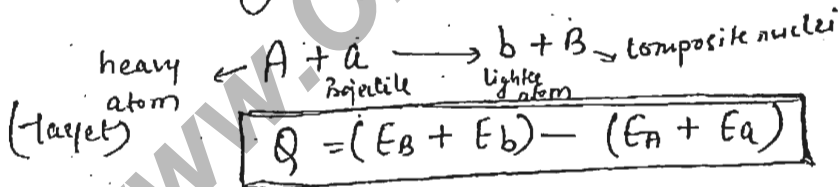
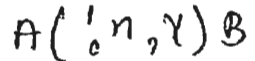
Q-value of Nuclear Reaction
 expressed in terms of incoming and outgoing kinetic energy.

$Q = +ve$	exoergic
$Q = -ve$	endoergic

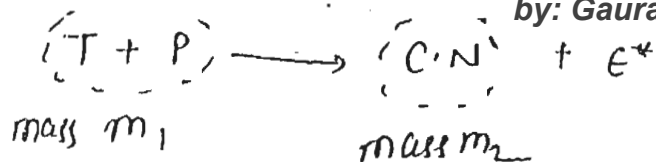
* \rightarrow Bethe's Notation



Neutron capture \rightarrow



$Q = -5.589$



If (i) $m_1 > m_2$ i.e. reactant mass is more, it is converting into K.E.

$$\therefore Q = \underline{\underline{+ve}}$$

(ii) $m_2 > m_1$; i.e. product mass is more
 \therefore K.E. is converting into mass

$$Q = \underline{\underline{-ve}}$$

When $m_1 > m_2$

$$\boxed{Q = \Delta m c^2} = (m_1 - m_2) c^2 \quad Q = \underline{\underline{+ve}}$$

(II) Momentum conservation

Momentum of projectile, P_p = momentum of $C \cdot N$

$$\boxed{P_p = P_{C \cdot N}}$$

from non-relativistic quantum, i.e. time independent quantum

$$\sqrt{2A_p E_p} = \sqrt{2A_{C \cdot N} E_{C \cdot N}}$$

$$A_p E_p = A_{C \cdot N} E_{C \cdot N}$$

$$\boxed{E_{C \cdot N} = \frac{A_p \cdot E_p}{A_{C \cdot N}}}$$

$$\begin{array}{l} P = \sqrt{2mE} \\ K.E. = \frac{P^2}{2m} \end{array}$$

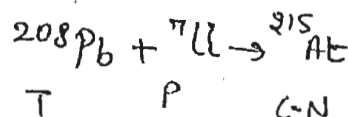
$$E_{p+q} = \frac{A_p}{A_{C \cdot N}} E_p + E^*$$

$$E_p \left[1 - \frac{A_p}{A_{C \cdot N}} \right] + Q = E^*$$

$$E_p \left[\frac{A_p + A_T - A_p}{A_{C \cdot N}} \right] = E^* - Q$$

$$\boxed{A_{C \cdot N} = A_p + A_T}$$

$$E_p \frac{A_T}{A_{C \cdot N}} = E^* - Q$$



$$E_p = (E^* - Q) \frac{A_C N}{A_T}$$

(i) When $E^* = 0 \Rightarrow E_p = E_{th}$

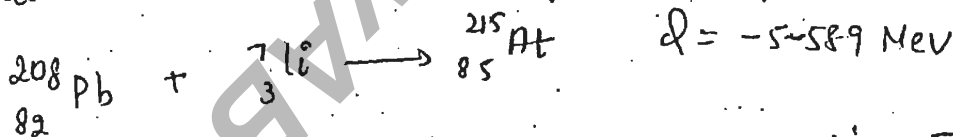
$$E_p = E_{th} = -Q \frac{A_C N}{A_T}$$

(ii) When $E^* \neq 0 \quad E^* = E_p \frac{A_T}{A_C N} + Q$

Hence threshold energy is greater than Q value with opposite sign always.

Excitation energy is then dissipated by emission of photon or nuclear particles.

Ques Calculate threshold energy and k.E. of $^{215}_{85}At$



- (i) 5.589 (ii) -5.77 (iii) 5.77 (iv) 5.377

Q k. opposite and greater value

$$E_{th} = -Q \frac{A_C N}{A_T} = -(-5.589) \times \frac{215}{208} = \underline{\underline{5.777 \text{ MeV}}}$$

$$E_{C.N} = E_p \frac{A_P}{A_C N}$$

$$E_p = -Q$$

i.e k.E of $^{215}_{85}At$

$5.58 \times \frac{7}{215} \rightarrow$ mass of projectile if we consider E^*

$$= 0.18 \text{ MeV}$$

$$E_p = (E^* - Q) \frac{A_C N}{A_T}$$

By putting E^* we get $E_p = -Q$

www.ChemistryABC.com, 5.58 MeV of K.E is by: ~~Gama~~ ^{Gamma} into mass, overcome the -ve. of value and 0.18 MeV goes into the K.E of composite nuclei.

$$E^* \propto T^2$$

$$E^* = aT^2$$

level density parameter.

Neutron activation Analysis :-

Instrumental NAA

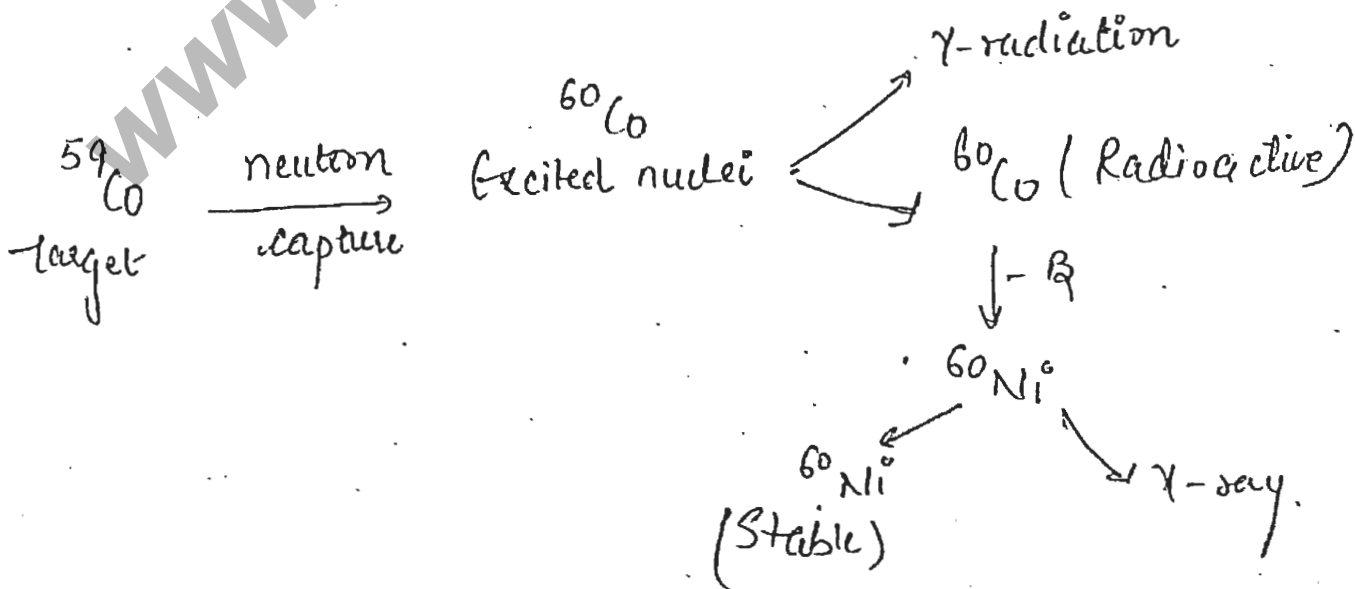
(Direct sample is used)

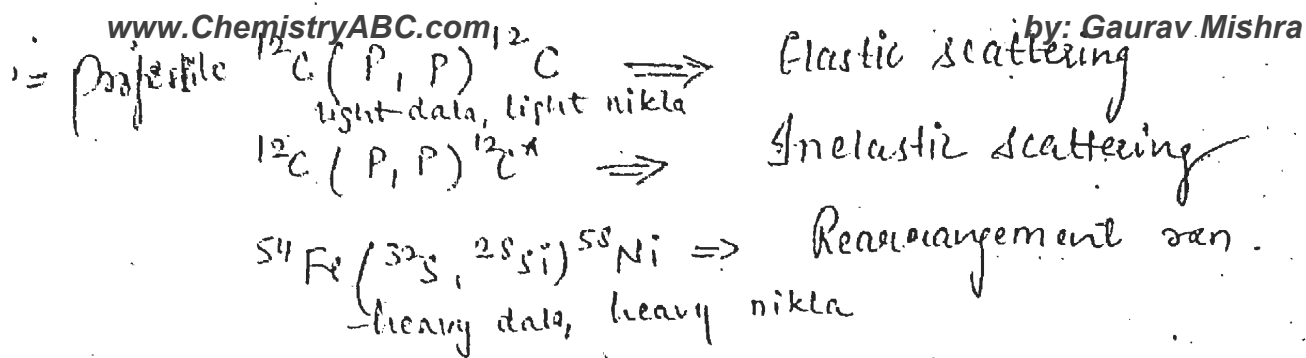
Nuclear process used to element. Sample is

causing the element to form radioactive isotopes

Radioactive emission and radiatively decay. path for each element are well known.

By this information we are it is possible to study emission spectra of radioactive sample and determine the conc. of element.





Area of cross section (σ)

Cross section area is related to probability that a rxn will take place.

$$\gamma = \phi_i n A t \sigma$$

γ = yield (no. of rxn per unit time)

n = particle density (no. of target particle per unit volume)

A = Area of beam spot

ϕ_i = Incidence flux $\left[\frac{\text{Beam particle}}{\text{time} \times \text{Area}} \right]$

t = thickness of target

σ also depends on half life of product

Nuclear fission (α -decay is nuclear fission)

Nucleus splits into two roughly equally sized fission fragments

$\frac{Z}{A} > 48$] \rightarrow Spontaneous Nuclear fission

$A > 220$] Spontaneous fission have low rate than α -decay